## 360. Molecular Polarisability. The Molar Kerr Constant of Ferrocene.

By M. Aroney, R. J. W. Le Fèvre, and K. M. Somasundaram.

From the viewpoint of polarisability ferrocene is equivalent to a krypton atom sandwiched between two planar regular-pentagonal $(\mathrm{CH})_{5}$ rings in each of which the carbon-carbon bond ellipsoids have the same semi-axes as those of the $\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}_{\mathrm{Ar}}$ bonds in benzene. On this basis the predicted molar Kerr constant is $20.1 \times 10^{-12}$, against a measured value of $19.9 \times 10^{-12}$.

The molar Kerr constants and total dielectric polarisations of ferrocene dissolved in carbon tetrachloride have been measured by standard methods ${ }^{1}$ at $25^{\circ}$. The observations listed below show the two properties mentioned to have values at infinite dilution of $19 \cdot 8_{7} \times$ $10^{-12}$ and $52 \cdot 4_{6}$ c.c. respectively. Since the molecular refraction (Na-d line) of ferrocene is 50.4 c.c. (so that ${ }_{\infty} P_{2}$ is slightly less than $1.05 R_{\mathrm{D}}$ ) the non-polarity of this molecule is confirmed. ${ }^{2}$

The molar Kerr constant is therefore controlled ${ }^{3}$ by the terms $\theta_{1}$ and $\theta_{3} ; \theta_{3}$ cannot be estimated a priori and, being probably small, will be neglected. From $\infty\left({ }_{m} K_{2}\right)=$ $19.87 \times 10^{-12}$ we have, ${ }^{4}$ therefore, $\theta_{1}=4.72_{5} \times 10^{-35}$, whence (with ${ }_{\mathrm{D}} P /{ }_{\mathrm{E}} P=1 \cdot 1$ ), $b_{1}-b_{3}= \pm 0.631 \times 10^{-23}$. It is assumed from the $X$-ray analyses of ferrocene ${ }^{5}$ that

[^0]the appropriate polarisability ellipsoid will be one of rotation, with semi-axes $b_{1}=b_{2}$, and $b_{3}$. Taking the electronic polarisation as $0.95 R_{\mathrm{D}}$ gives $2 b_{1}+b_{3}=5.691 \times 10^{-23}$. By experiment two alternative solutions thus become available:

|  |  | $10^{46}\left(b_{1}-b_{3}\right)^{2}$ | $10^{23} b_{1}$ |
| :--- | :---: | :---: | :---: |
| Solution A $\ldots \ldots \ldots \ldots \ldots \ldots$. | $0 \cdot 398$ | $2 \cdot 107$ | $10^{23} b_{3}$ |
| Solution B $\ldots \ldots \ldots \ldots \ldots \ldots$ | 0.398 | 1.687 | 2.476 |
|  |  |  |  |

According to A , ferrocene is more polarisable in planes parallel to the pentagonal rings than in directions perpendicular to them; according to $B$, the reverse is true.

No direct evidence exists to guide a choice between A and B. Previously ${ }^{6}$ it has been noted that the dimensions of the " cavity " created by a solute in its solvent often provide data with which to divide ( $b_{1}+b_{2}+b_{3}$ ) into the separate components. Using the distances $\mathrm{C}-\mathrm{C}=1.40 \AA, \mathrm{C}-\mathrm{Fe}=2.044 \AA$ (as cited in Pauson's review ${ }^{5}$ ), and $\mathrm{C}-\mathrm{H}=1.04$ $\AA$, and adopting $108^{\circ}$ as the $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angle, together with " Wirkungsradien " from Stuart ${ }^{7}$ (i.e., following the procedures of past studies ${ }^{8}$ of the dielectric polarisation-medium effect), gives a model containable within a cylinder of height $6 \cdot 2 \AA$ and diameter $6 \cdot 3 \AA$. Solution A is thus favoured, although the anisotropy forecast is much less than that observed.

A more satisfactory approach is to note that the $\mathrm{C}-\mathrm{C}$ distance is equal to that which occurs in benzene, so that-since bond lengths and bond polarisabilities are connected ${ }^{9}$ -$\mathrm{C}_{\mathrm{Ar}}-\mathrm{C}_{\mathrm{Ar}}$ ellipsoids may be applied to the $\mathrm{C}_{5}$ rings of ferrocene. As the $\mathrm{C}-\mathrm{H}$ link is isotropically polarisable, ${ }^{10}$ an ellipsoid for the ( $\left.\mathrm{CH}-\mathrm{CH}\right)_{\text {aromatic }}$ unit may be used. Benzene ${ }^{11}$ has ${ }_{\infty}\left({ }_{m} K_{2}\right)=7 \cdot 2_{4} \times 10^{-12}$ at $20^{\circ}$; this with ${ }_{\mathrm{E}} P=25 \cdot 0_{3}$ c.c. gives $b_{1} \mathrm{C}_{\mathrm{E}} \mathrm{H}_{6}=b_{2} \mathrm{C}_{6} \mathrm{H}_{6}=1 \cdot 12_{0} \times$ $10^{-23}$, and $b_{3}{ }^{\mathrm{C}_{6} \mathrm{H}_{6}}=0.73_{6} \times 10^{-23} ; b_{\mathrm{V}}{ }^{\text {(CH.CH)Ar }}$ therefore is $0.123 \times 10^{-23}$. By Le Fèvre's equation, ${ }^{9} 10^{23} b_{\mathrm{L}}{ }^{(\mathrm{CH} \cdot \mathrm{OH}) \mathrm{Ar}}$ is $0 \cdot 288 ; b_{\mathrm{L}}+b_{\mathrm{T}}+b_{\mathrm{V}}$ for $(\mathrm{CH} \cdot \mathrm{CH})_{\mathrm{Ar}}$ is $1 / 6$ of $2 b_{1}+b_{3}$ for benzene; by difference $b_{\mathrm{T}}$ (OH.CR)Ar is therefore $0.085 \times 10^{-23}$. Utilising these semi-axes for a regular pentagonal $(\mathrm{CH})_{5}$ ring gives $0.932,0.932$, and $0.615 \times 10^{-23}$ respectively for $b_{1}{ }^{(\mathrm{CH})_{s},} b_{2}{ }^{(\mathrm{CHH})_{s}}$, and $b_{3}{ }^{(\mathrm{CHH})_{5}}$. As there are two parallel $(\mathrm{CH})_{5}$ rings in ferrocene, the $\theta_{1}$ for this molecule should contain a contribution from these rings of $\left(b_{1}-b_{3}\right)^{2}=0.402 \times 10^{-46}$; this is very close to the quantity ( $0.398 \times 10^{-46}$ ) observed; the calculated ${ }_{m} K$ from this factor alone is $20.1 \times 10^{-12}$; the ${ }_{\mathrm{m}} K$ from experiment is $19.9 \times 10^{-12}$.

The implication is that the iron atom is nearly isotropic in its polarisability. Algebraically positive semi-axes for the iron atom can be estimated only from solution A (which is therefore preferable to B ) ; they are:

Across the $(\mathrm{CH})_{5}$ planes: $2.107-2 \times 0.932=0.243 \times 10^{-23}$
At $90^{\circ}$ to the $(\mathrm{CH})_{5}$ planes: $1.476-2 \times 0.615=0.246 \times 10^{-23}$
Such values for iron are of interest in regard to suggestions ${ }^{5}$ that the iron atom in ferrocene has the electronic configuration of krypton, for which gas Watson and Ramaswamy ${ }^{12}$ (from refractivity-dispersion measurements) recorded an electronic polarisation of $6 \cdot 26$ c.c; from this, treating krypton as an isotropically polarisable atom, we obtain $b_{1} \mathrm{Kr}=$ $b_{2}{ }^{\mathrm{Kr}}=b_{3}{ }^{\mathrm{Kr}}=0.248 \times 10^{-23}$. To emphasise the significance of these conclusions: had we assumed a priori that ferrocene is equivalent to a krypton atom sandwiched between two parallel $(\mathrm{CH})_{5}$ planes, the $b_{1}$ and $b_{3}$ expected would have been $2 \cdot 112 \times 10^{-23}$ and $1.478 \times 10^{-23}$, and the ${ }_{\mathrm{m}} K_{\text {cale. }}$ only $c a .0 .2 \times 10^{-12}$ higher than that in fact found.

[^1]
## Experimental

Ferrocene, m. p. $173-174^{\circ}$, was prepared as described by Wilkinson ${ }^{13}$ except that the crude product was distilled in steam and recrystallised from aqueous methanol.

Measurements of the following properties of solutions containing weight fractions $w_{2}$ of solute in carbon tetrachloride have been made at $25^{\circ}: \Delta B$, differences between Kerr constants of solution and solvent, $\Delta n$, differences between refractive indexes ( Na light) of solution and solvent, $\varepsilon_{12}$ and $d_{12}$, the dielectric constants and densities respectively. For $w_{2}=0, B=$ $0.070 \times 10^{-7}, n_{\mathrm{D}}=1.4575, \varepsilon=2.2270$, and $d=1.58454$. Details concerning procedures, calculations, etc., are given in ref. 1.

Observations on ferrocene-carbon tetrachloride solutions at $25^{\circ}$.

| $10^{5} w_{2}$ | 1046 | 1292 | 1426 | 1434 | 1671 | 1909 | 1924 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $10^{7} \Delta B$ | 0.0115 | $0.014_{5}$ | $0 \cdot 0158$ | 0.016 ${ }_{1}$ | $0 \cdot 019{ }_{4}$ | 0.022 ${ }_{5}$ | $0 \cdot 023_{3}$ |
| $10^{4} \Delta n$ | 22 | 27 | 29 | 30 | 35 | 40 | 41 |
| $\varepsilon_{12}$ | $2 \cdot 2335$ | 2.2349 | $2 \cdot 2360$ | $2 \cdot 2363$ | $2 \cdot 2374$ | 2.2388 | $2 \cdot 2392$ |
| $d_{12}$ | 1.58124 | 1.58104 | 1.58086 | 1.58030 | 1.57979 | $1 \cdot 57956$ | 1.57902 |

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University of Sydney, N.S.W., Australia.
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${ }^{13}$ Wilkinson, Org. Synth., 1956, 36, 31.


[^0]:    ${ }^{1}$ (a) Le Fèvre and Le Fèvre, $J ., 1953,4041$; 1954, 1577; (b) Rev. Pure Appl. Chem., 1955, 5, 261 ; (a) Le Fèvre, " Dipole Moments," Methuen, London, 3rd edn., 1953, Chap. 2.
    ${ }_{2}$ Wilkinson, Rosenblum, Whiting, and Woodward, J. Amer. Chem. Soc., 1952, 74, 2125.
    ${ }^{3}$ Ref. $1(b)$, pp. 286, 309.
    ${ }^{4}$ Ref. l(b), p. 270.
    ${ }^{5}$ Pauson, Quart. Rev., 1955, 9, 391.

[^1]:    ${ }^{6}$ Ref. 2, p. 287; Le Fèvre and Le Fèvre, $J ., 1955,2750 ;$ Le Fèvre, Le Fèvre, Rao, and Smith, $J$., 1959, 1188.
    ${ }^{7}$ Stuart, Z. phys. Chem., 1935, B, 2\%, 350.
    ${ }^{8}$ Ref. 1 (c), Chap. 3.
    ${ }^{9}$ Le Fèvre, Proc. Chem. Soc., 1958, 283.
    ${ }^{10}$ Le Fèvre and Le Fèvre, Chem. and Ind., 1955, 1121; cf. ref. 1(b), p. 299.
    ${ }^{11}$ Ref. $1(a), 1954$; cf. ref. $1(b)$, p. 284.
    ${ }^{12}$ Watson and Ramaswamy, Proc. Roy. Soc., 1936, A, 156, 144.

